

# Opportunistic Information Dissemination in Mobile Ad-hoc Networks: The Profit of Global Synchrony

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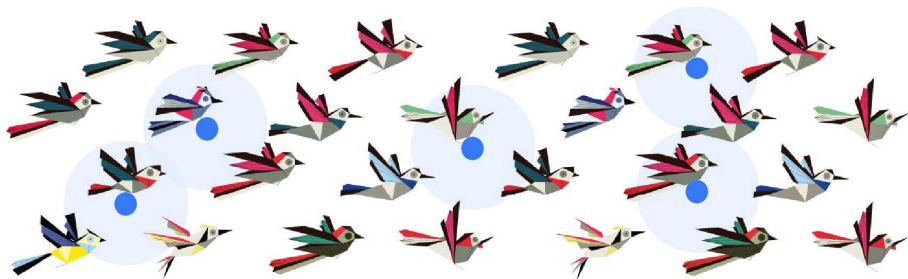
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- Mobile set of nodes (processors with radio)
- No stable communication infrastructure
- Multihop network

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E.g.



# Opportunistic Communication

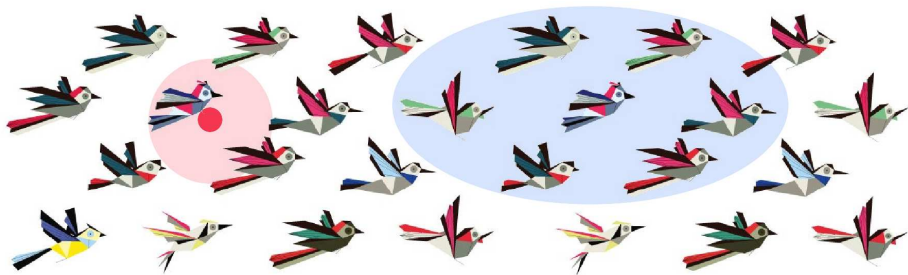
Thanks to mobility and asynch activation  
communication between  $x$  and  $y$  is feasible  
even if a path never exists! (*online route*)

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e.g. delay/disruption tolerant networks, opportunistic networking, etc.

# The Dissemination Problem

Some information held by a given source node  $x$  at time  $t$ ,  
must be disseminated to all nodes satisfying a given predicate  $\mathcal{P}$ .



Notation:

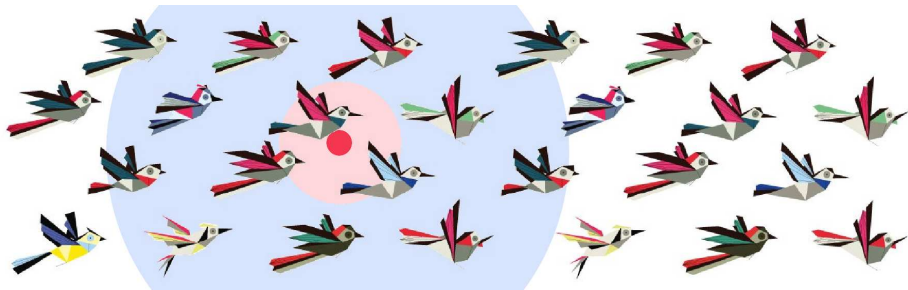
- a node that has received the information is *covered* (may be off)
- a node that holds the information is *informed*

# The Dissemination Problem

$\mathcal{P} \implies$  Dissemination  $\equiv$  Broadcast, Geocast, Multicast, Routing, etc.

In order to prove lower bounds we use **Geocast**:

$\mathcal{P}(y) = \text{true}$  iff, at time  $t$ ,  
 $y$  is active and located within distance  $d$  of  $x$ .



$d$  and  $t$  are parameters.

# Model

- Network:

- $n$  mobile nodes deployed in  $\mathbb{R}^2$
- slotted time steps:
  - slot length dominated by communication time
  - same for all nodes

- Node:

- unique ID in  $[n]$
- may start/fail at any time slot
- radio communication:
  - unique radio channel  $\implies$  collisions
  - background noise  $\equiv$  collision noise  $\implies$  no collision detection
  - no simultaneous reception & transmission
  - limited range  $r \implies$  multihop network

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  - de/activation schedule (many of our lb's don't even use it)
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But, worst-case adversarial topologies

$\implies$   $\nexists$  deterministic Broadcast protocol,  
even if connectivity is guaranteed! [CPMS'07]  
 $\implies$  adversary **must** be limited.

# Model

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limited by three parameters:

- a maximum speed  $v_{\max} > 0$
- the system must be  $(\alpha, \beta)$ -connected,  $\alpha, \beta \in \mathbb{Z}^+$

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in words:

- while moving at  $\leq v_{\max}$  speed,
- $\leq \alpha$  steps disconnected (w.r.t. progress)
- $\geq \beta$  steps pair-stability (to allow progress)

( $\beta \implies$  impossibility results,  $\alpha \implies$  time complexity)

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## Definition

Given a MANET and an instance of Dissemination, the system is  $(\alpha, \beta)$ -connected if,  $\forall t \exists t'$ :

- $[t, t + \alpha) \cap [t', t' + \beta) \neq \emptyset$
- $\exists$  nodes  $x, y$ :  $x$  is informed and  $y$  is uncovered at time  $t'$ :  
 $x, y$  are active neighbors during  $[t', t' + \beta)$ .

# Model

$(\alpha, \beta)$ -connectivity

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# Model

- Protocols:
  - oblivious protocol [K'05,KP'05]: use **only** node ID and time elapsed since node activation.
  - quasi-oblivious protocol [PR'09]: use also the global time.
  - adaptive protocol: no restriction.

We assume that uninformed nodes do not transmit.

# Related Work

Dissemination problems studied:

Broadcast, Geocast,  $k$ -Selection, Multicast, Gossiping, etc.

But, deterministic solutions rely on strong synchronization or stability:

- deterministic Broadcast in MANET [MCSPS'06].  
(One-dimension, known position.)
- deterministic Multicast in MANET [GS'99, PR'97].  
(Long enough globally stable topology periods.)

Leaving aside channel contention:

- Broadcast in MANET
  - $\Omega(n)$  rounds [PSMCS'04], even if nodes move in a grid.
  - $\Omega(D \log n)$  [BD'97].
  - $\Omega(n \log n)$  in [DP'07]. (linear  $D$ )
- Geocast in MANET [FM'08].



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# Results

- $\forall$  Geocast ... protocol:  $\exists (\alpha, \beta)$ -conn MANET:

using only arbitrarily slow movements:

$$\text{even random} \rightarrow \geq \alpha(n-1), v_{\max} > 0$$

using only activation:

$$\text{(equi)periodic} \rightarrow \geq n(n-1)/2, v_{\max} \geq 0$$

# Results

- $\forall$  Geocast ... protocol:  $\exists (\alpha, \beta)$ -conn MANET:

using adversarial activation:

$$\text{oblivious} \quad \left\{ \begin{array}{ll} \Omega\left(\alpha n + \frac{n^3}{\log n}\right) & v_{\max} \in \Omega\left(\frac{\pi r}{\alpha + n^2 / \log n}\right) \\ \beta \in \Omega\left(\frac{n^2}{\log n}\right) & v_{\max} > 0 \end{array} \right.$$

even with simultaneous activation and no failures:

$$\text{adaptive} \quad \left\{ \begin{array}{ll} \Omega(\alpha n + n^2) & v_{\max} \in \Omega\left(\frac{\pi r}{\alpha + n}\right) \\ \beta \geq n - 1 & v_{\max} > 0 \end{array} \right.$$

- Dissemination protocols:

oblivious  $\rightarrow \alpha n + O(n^3 \log n)$ ,  $\beta \in \Omega(n^2 \log n)$ . (Primed-Selection.)

quasi-oblivious  $\rightarrow \alpha n + n^2$ ,  $\beta \geq n$ . (Round-Robin, piggybacking a counter.)

# Lower Bounds

By pigeonhole principle:

## Lemma

*For any time step  $t$  of the execution of a Dissemination protocol, where a subset  $V'$  of  $k$  informed nodes do not fail during the interval  $[t, t + k - 2]$ , there exists some node  $v \in V'$  such that  $v$  does not transmit uniquely among the nodes in  $V'$  during the interval  $[t, t + k - 2]$ .*

By probabilistic method:

## Lemma

*For any deterministic oblivious protocol that solves Dissemination in a MANET of  $n$  nodes, where nodes are activated possibly at different times, and for any subset of  $k$  nodes,  $k \geq 3$ , there exists a node-activation schedule such that, for any time slot  $t$  and letting  $m = \lfloor k(k-1)/\ln(k(k-1)) \rfloor$ , each of the  $k$  nodes is activated during the interval  $[t - m + 1, t]$ , and there is one of the  $k$  nodes that is not scheduled to transmit uniquely among those  $k$  nodes during the interval  $[t, t + m - 1]$ .*

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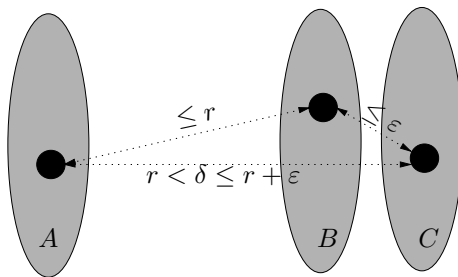
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# Lower Bounds

## Theorem

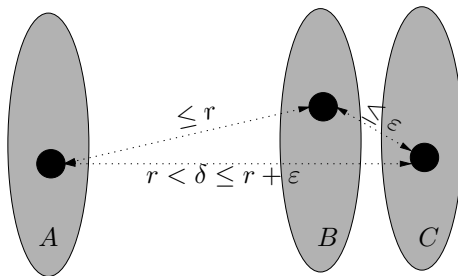
For any  $V_{max} > 0$ ,  $d > r$ ,  $\alpha > 0$ , and any deterministic Geocast protocol  $\Pi$ , if  $\beta < n - 1$ , there exists an  $(\alpha, \beta)$ -connected MANET of  $n$  nodes such that  $\Pi$  does not terminate, even if all nodes are activated simultaneously and do not fail.



# Lower Bounds

## Theorem

For any  $V_{max} > 0$ ,  $d > r$ ,  $n \geq 8$ ,  $\alpha > 0$ , and any deterministic oblivious protocol for Geocast  $\Pi$ , if  $\beta \leq m = \lfloor (n-1)(n-3)/(4 \ln((n-1)(n-3)/4)) \rfloor$ , there exists an  $(\alpha, \beta)$ -connected MANET of  $n$  nodes such that  $\Pi$  does not terminate.



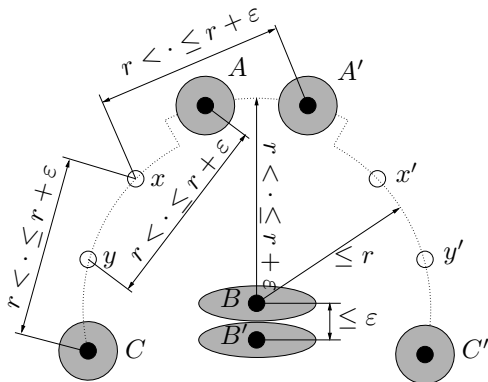


# Lower Bounds

## Theorem

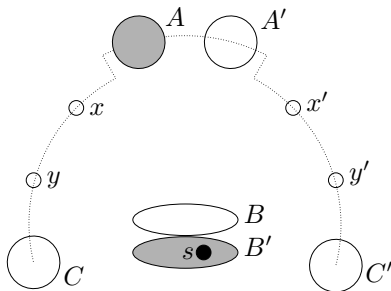
For any  $v_{max} > \pi r / (3(2\alpha + n - 4))$ ,  $d > r$ ,

$\forall$  deterministic Geocast protocol:  $\exists(\alpha, \beta)$ -connected MANET:  $\Omega(\alpha n + n^2)$ .

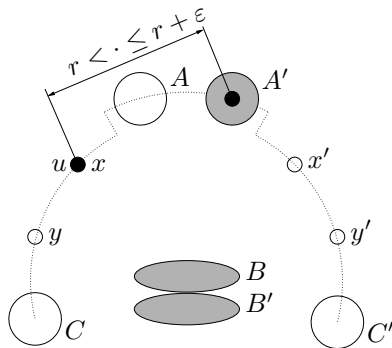
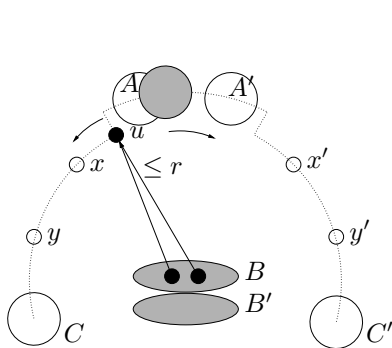


# Lower Bounds

Initial configuration

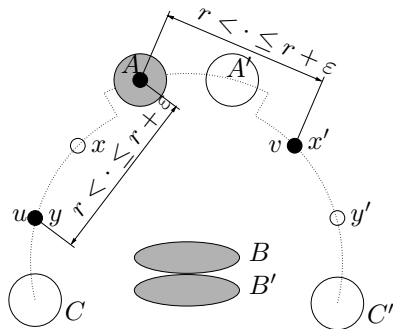
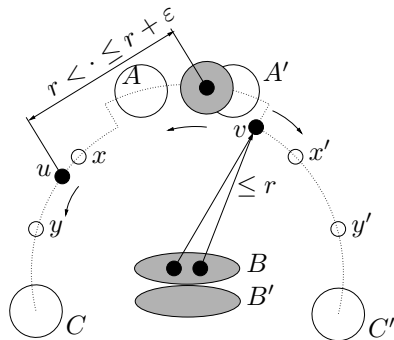


# Lower Bounds



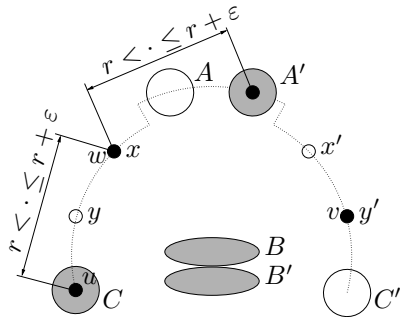
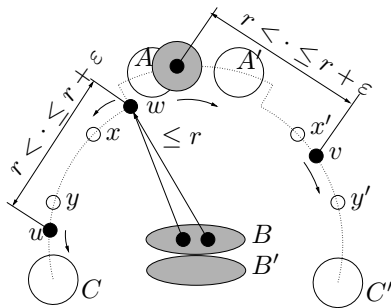
(b) End of phase 1 of  $u$

## Lower Bounds



(d) End of phase 2 of  $u$  and phase 1 of  $v$

# Lower Bounds

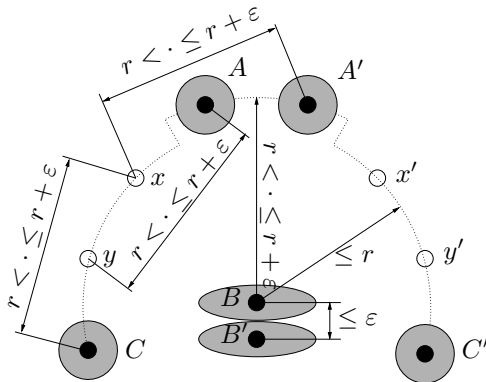


(f) End of phase 3 of  $u$ , phase 2 of  $v$ , and phase 1 of  $w$

# Lower Bounds

## Theorem

For any  $v_{max} > \pi r/6(\alpha + \lfloor (n/3)(n/3 - 1)/\ln(n/3(n/3 - 1)) \rfloor - 2)$ ,  $d > r$ ,  $n \geq 9$ ,  
 $\forall$  *oblivious* deterministic Geocast protocol:  $\exists(\alpha, \beta)$ -connected MANET:  
 $\Omega(\alpha n + n^3/\log n)$ .



# Conclusions

## Profit of global synchrony:

- full adaptiveness ( $\Omega(\alpha n + n^2)$ )  
does not help w.r.t. quasi-obliviousness ( $\alpha n + n^2$ ).
- almost linear separation between oblivious ( $\Omega(\alpha n + n^3 / \log n)$ )  
and quasi-oblivious protocols ( $\alpha n + n^2$ ).
- while  $\beta = n$  is enough for quasi-oblivious,  
oblivious protocols require  $\beta \in \Omega(n^2 / \log n)$ .

Thank you