

# Internet Computing: Using Reputation to Select Workers from a Pool

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# Internet-based task computing

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- Growing use and capabilities of personal computers.
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## Internet emerges as a viable platform:

- Grid and cloud computing.  
e.g. EGEE Grid, TERA Grid, Amazon's EC2
- Volunteering computing.  
e.g. SETI@home, AIDS@home, Folding@home
- Crowd computing.  
e.g. Amazon Mechanical Turk (human based-computing)

# SETI@home by the numbers

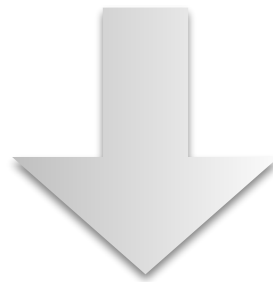
As reported in November 2009:

- 278,832 active CPUs (out of a total of 2.4 million) in 234 countries.
- 769 TFLOPs.

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Proc. power comparable with supercomputers,  
at a fraction of the cost!

Great potential **limited by untrustworthy entities.**

# Internet-based task computing

A more dynamic and unpredictable setting:

- Number of tasks is not fixed or known a priori:
  - It may be anything from **one** to **many**, even unbounded.
  - Tasks arrive dynamically and continuously.
- Dynamic participation:
  - Participating processors (workers) could change over time, not only due to failures.
- Increased frequency of failures:
  - Failures are the norm rather than the exception.

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**A whole new world to study tradeoffs between efficiency and fault tolerance!**

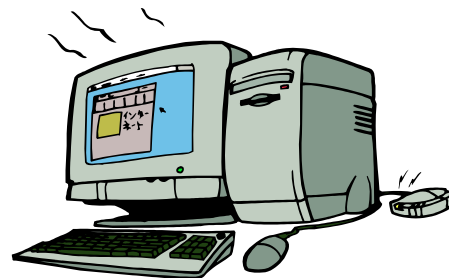
# Master-worker computing

Master



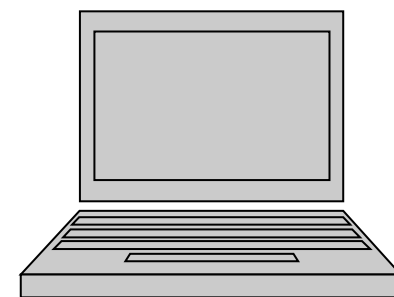
Worker

...



Worker

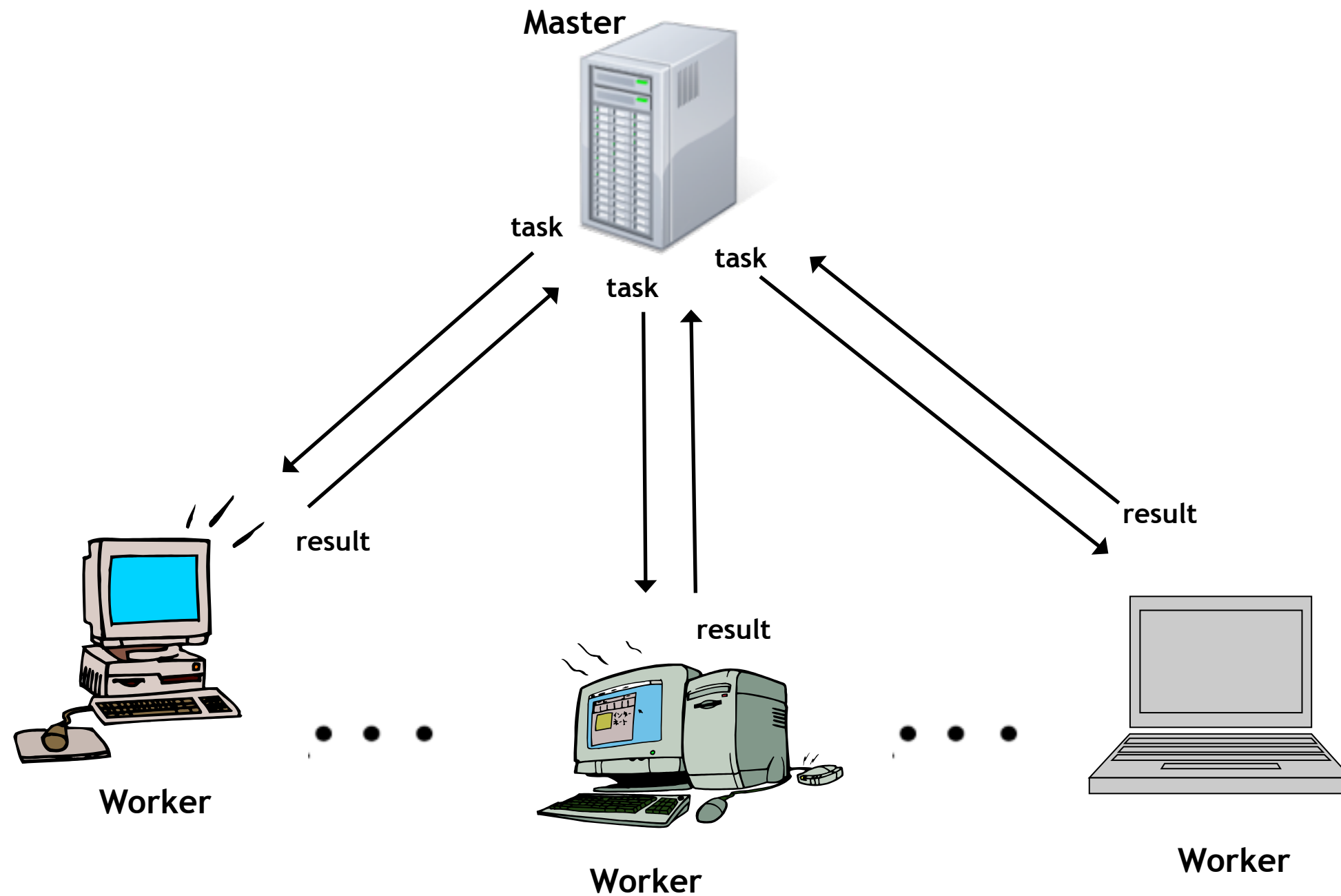
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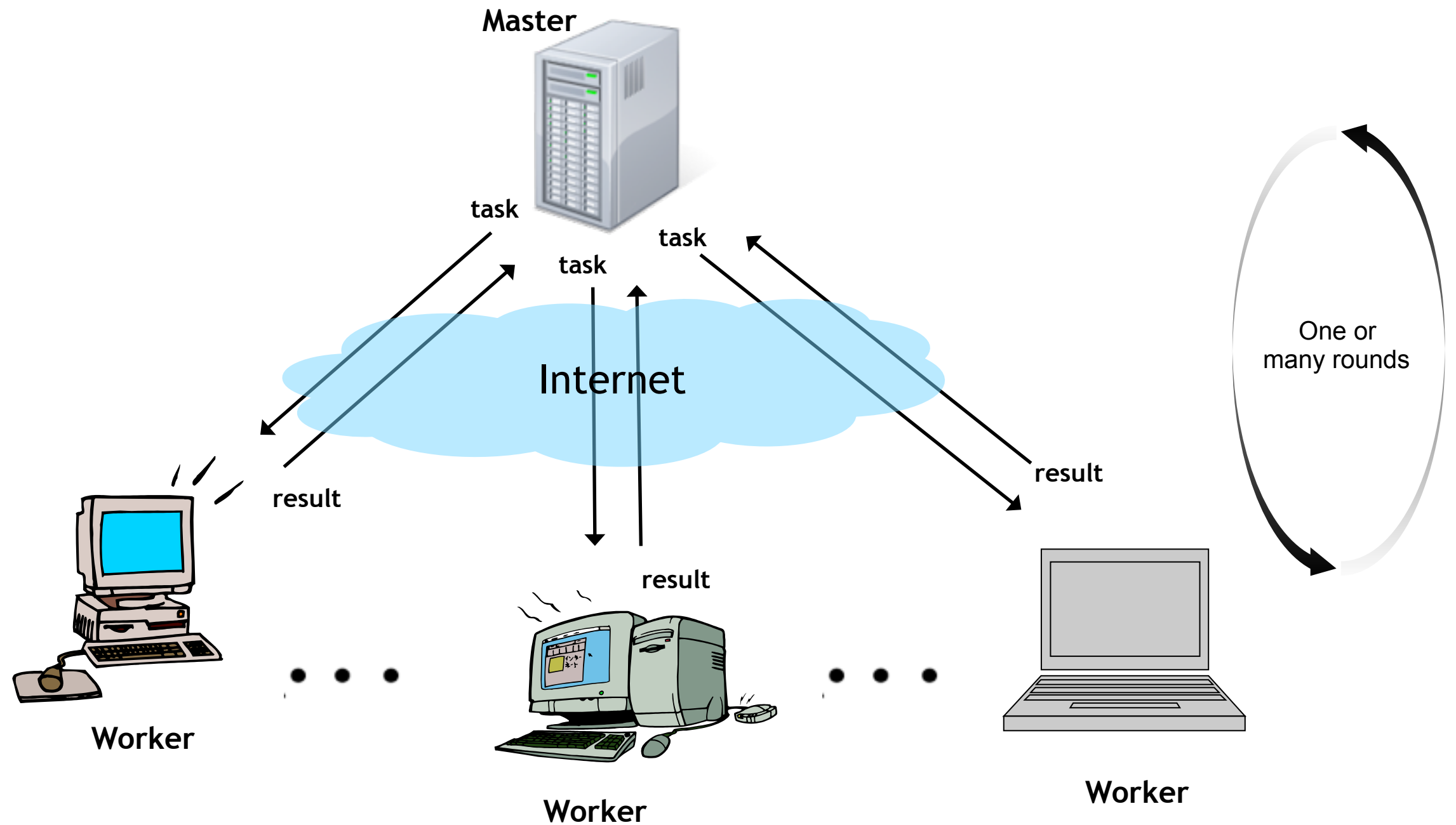
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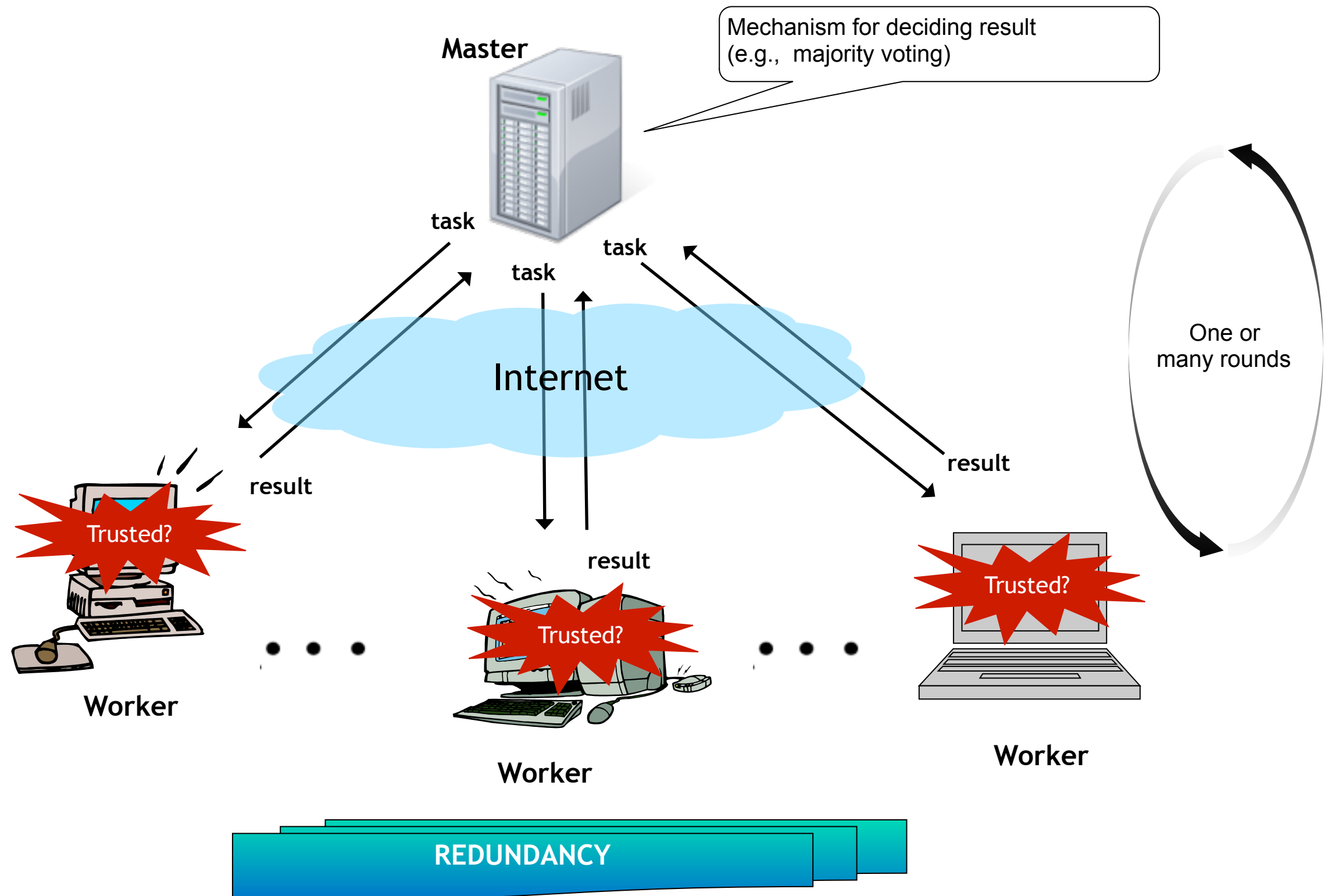
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# Types of workers

## Classical distributed computing approach:

- **Malicious** workers: **always** return a fabricated **incorrect** result.
- **Altruistic** workers: **always** compute and return a **correct** result.

[Fernandez-Anta et al.; Konwar; Sarmenta]

## Game theoretical approach:

- **Rational** workers: choose the strategy that maximizes benefit.

[Abraham et al;Golle et al;Shneidman et al; Yurkewych;NCA'08;PLOS One'15]

## All three types considered:

- **Mechanisms with reward/punishment schemes** that
  - provide incentives for rationals to be honest
  - cope with malicious actions.

[IPDPS'10;NCA'11;DISC'11;TC'14]

# Rewards/punishments

$WP_C$	worker punishment for being caught cheating
$WC_T$	worker cost of computing the task
$WB_Y$	worker benefit from master acceptance
$MC_Y$	master cost for accepting the worker answer
$MC_A$	master cost for auditing worker answer
$MB_R$	master benefit from accepting the correct answer
$MP_W$	master punishment for accepting a wrong answer

# Task computing scheme

- Master assigns a task to  $n$  workers.
- Workers:
  - Malicious: fabricates a result.
  - Altruistic: computes the result.
  - Rational: cheats with probability  $p_C$ .
- Master audits with probability  $p_A$ .
- If master audits:
  - computes the task.
  - rewards honest workers and penalizes cheaters.
- If master does not audit:
  - accepts value returned by “majority” of workers.
  - rewards those in the “majority”.

# Types of computations

## One-shot

- Model the decisions (cheat or not, audit or not) as a **game**.
- Find conditions on the parameters for **Nash equilibria**.
- The  $p_C$ ,  $p_A$ , and  $n$  obtained yield correctness at low cost for the master, even in presence of malice.
- **Trade-off**: probability of correct vs. cost.
- **Constrains**: **malice**, **collusion**, **unreliable communication**.

[NCA'08;IPDPS'10;DISC'11;NCA'11;TC'14, PLOS One'15]

## Multi-round

- **Evolutionary dynamics**:  $p_C$  and  $p_A$  updated after each round ( $n$  is fixed).
- **Reinforcement learning**: update function of worker profit aspiration and master tolerance to loss.
- Objective: eventual correctness.
- **Trade-off**: time to correct vs. cost.
- **Constrains/features**: **malice**, **unreliable communication**, **reputation system**.

[PODC'12, EUROPAR'12, OPODIS'13, JOSS'13, CCPE'13]

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But, workers may not be available all the time!  
Why not taking advantage of  $N \gg n$ ? (Internet scale)



# Our contributions

- We present a mechanism that
  1. it is resilient to non-responsive and unreliable workers:
    - *responsiveness reputation*: replies/assignments ratio.
    - 3 *truthfulness reputations*: ~BOINC, [OPODIS'13], [Sonnek et al.].
  2. leverages availability of  $N \gg n$  workers:

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showing pools of workers such that eventual correctness

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- We study feasibility in absence of rationals:

showing pools of workers such that eventual correctness

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  - achieved forever with minimal auditing.
- Experimental evaluation:

complements analysis for scenarios where rational workers exist.  
reputation-types comparison showing reliability/cost trade-offs.

# Types of reputation

- Responsiveness:

$$\rho(w) = \frac{\text{replies}(w) + 1}{\text{assignments}(w) + 1}$$

- Truthfulness:

LINEAR:

[Sonnek et al.]

$$\rho(w) = \frac{\text{audited-correct}(w) + 1}{\text{audited}(w) + 1}$$

EXPONENTIAL:

[OPODIS'13]

$$\rho(w) = \frac{\kappa^{\text{audited-correct}(w)}}{\kappa^{\text{audited}(w)}}, \kappa > 1$$

BOINC:

$$\rho(w) = 1 - \frac{1}{\text{streak}(w)} \quad (0 \text{ if } \text{streak}(w) < 10)$$

# Protocol

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**Algorithm 1** Master's Algorithm

---

```
1   $p_{\mathcal{A}} \leftarrow x$ , where  $x \in [p_{\mathcal{A}}^{min}, 1]$ 
2  for  $i \leftarrow 0$  to  $N$  do
3       $select_i \leftarrow 0$ ;  $reply\_select_i \leftarrow 0$ ;  $audit\_reply\_select_i \leftarrow 0$ ;  $correct\_audit_i \leftarrow 0$ ;  $streak_i \leftarrow 0$ 
4       $\rho_{rs_i} \leftarrow 1$ ; initialize  $\rho_{tr_i}$  // initially all workers have the same reputation
5  for  $r \leftarrow 1$  to  $\infty$  do
6       $W^r \leftarrow \{i \in \mathcal{N} : i \text{ is chosen as one of the } n \text{ workers with the highest } \rho_i = \rho_{rs_i} \cdot \rho_{tr_i}\}$ 
7       $\forall i \in W^r : select_i \leftarrow select_i + 1$ 
8      send a task  $T$  to all workers in  $W^r$ 
9      collect replies from workers in  $W^r$  for  $t$  time
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11      $R \leftarrow \{i \in W^r : \text{a reply from } i \text{ was received by time } t\}$ 
12      $\forall i \in R : reply\_select_i \leftarrow reply\_select_i + 1$ 
13     update responsiveness reputation  $\rho_{rs_i}$  of each worker  $i \in W^r$ 
14     audit the received answers with probability  $p_{\mathcal{A}}$ 
15     if the answers were not audited then
16         accept the value  $m$  returned by workers  $R_m \subseteq R$ ,
17         where  $\forall m', \rho_{tr_{R_m}} \geq \rho_{tr_{R_{m'}}$  // weighted majority of workers in  $R$ 
18     else // the master audits
19         foreach  $i \in R$  do
20              $audit\_reply\_select_i \leftarrow audit\_reply\_select_i + 1$ 
21             if  $i \in F$  then  $streak_i \leftarrow 0$  //  $F \subseteq R$  is the set of responsive workers caught cheating
22             else  $correct\_audit_i \leftarrow correct\_audit_i + 1$ ,  $streak_i \leftarrow streak_i + 1$  // honest responsive
23             update truthfulness reputation  $\rho_{tr_i}$  // depending on the type used
24             if  $\rho_{tr_R} = 0$  then  $p_{\mathcal{A}} \leftarrow \min\{1, p_{\mathcal{A}} + \alpha_m\}$ 
25             else
26                  $p'_{\mathcal{A}} \leftarrow p_{\mathcal{A}} + \alpha_m(\rho_{tr_F} / \rho_{tr_R} - \tau)$ 
27                  $p_{\mathcal{A}} \leftarrow \min\{1, \max\{p_{\mathcal{A}}^{min}, p'_{\mathcal{A}}\}\}$ 
28      $\forall i \in W^r : \text{return } \Pi_i$  to worker  $i$  // the payoff of workers in  $W^r \setminus R$  is zero
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---

# Protocol

for each  
round of  
computation

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# Protocol

select  
workers  
according to  
reputation

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# Protocol

send task  
and collect  
replies

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update  
responsiveness  
reputation

# Protocol

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---

audit with  
probability  $p_A$

# Protocol

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```
1   $p_A \leftarrow x$ , where  $x \in [p_A^{min}, 1]$ 
2  for  $i \leftarrow 0$  to  $N$  do
3       $select_i \leftarrow 0$ ;  $reply\_select_i \leftarrow 0$ ;  $audit\_reply\_select_i \leftarrow 0$ ;  $correct\_audit_i \leftarrow 0$ ;  $streak_i \leftarrow 0$ 
4       $\rho_{rs_i} \leftarrow 1$ ; initialize  $\rho_{tr_i}$  // initially all workers have the same reputation
5  for  $r \leftarrow 1$  to  $\infty$  do
6       $W^r \leftarrow \{i \in \mathcal{N} : i \text{ is chosen as one of the } n \text{ workers with the highest } \rho_i = \rho_{rs_i} \cdot \rho_{tr_i}\}$ 
7       $\forall i \in W^r : select_i \leftarrow select_i + 1$ 
8      send a task  $T$  to all workers in  $W^r$ 
9      collect replies from workers in  $W^r$  for  $t$  time
10     wait for  $t$  time collecting replies as received from workers in  $W^r$ 
11      $R \leftarrow \{i \in W^r : \text{a reply from } i \text{ was received by time } t\}$ 
12      $\forall i \in R : reply\_select_i \leftarrow reply\_select_i + 1$ 
13     update responsiveness reputation  $\rho_{rs_i}$  of each worker  $i \in W^r$ 
14     audit the received answers with probability  $p_A$ 
15     if the answers were not audited then
16         accept the value  $m$  returned by workers  $R_m \subseteq R$ ,
17         where  $\forall m', \rho_{tr_{R_m}} \geq \rho_{tr_{R_{m'}}$  // weighted majority of workers in  $R$ 
18     else // the master audits
19         foreach  $i \in R$  do
20              $audit\_reply\_select_i \leftarrow audit\_reply\_select_i + 1$ 
21             if  $i \in F$  then  $streak_i \leftarrow 0$  //  $F \subseteq R$  is the set of responsive workers caught cheating
22             else  $correct\_audit_i \leftarrow correct\_audit_i + 1$ ,  $streak_i \leftarrow streak_i + 1$  // honest responsive
23             update truthfulness reputation  $\rho_{tr_i}$  // depending on the type used
24             if  $\rho_{tr_R} = 0$  then  $p_A \leftarrow \min\{1, p_A + \alpha_m\}$ 
25             else
26                  $p'_A \leftarrow p_A + \alpha_m(\rho_{tr_F} / \rho_{tr_R} - \tau)$ 
27                  $p_A \leftarrow \min\{1, \max\{p_A^{min}, p'_A\}\}$ 
28      $\forall i \in W^r : \text{return } \Pi_i \text{ to worker } i$  // the payoff of workers in  $W^r \setminus R$  is zero
```

---

if NOT audited,  
accept majority  
weighted by  
truthfulness rep

# Protocol

---

**Algorithm 1** Master's Algorithm

---

```
1   $p_A \leftarrow x$ , where  $x \in [p_A^{min}, 1]$ 
2  for  $i \leftarrow 0$  to  $N$  do
3       $select_i \leftarrow 0$ ;  $reply\_select_i \leftarrow 0$ ;  $audit\_reply\_select_i \leftarrow 0$ ;  $correct\_audit_i \leftarrow 0$ ;  $streak_i \leftarrow 0$ 
4       $\rho_{rs_i} \leftarrow 1$ ; initialize  $\rho_{tr_i}$  // initially all workers have the same reputation
5  for  $r \leftarrow 1$  to  $\infty$  do
6       $W^r \leftarrow \{i \in \mathcal{N} : i \text{ is chosen as one of the } n \text{ workers with the highest } \rho_i = \rho_{rs_i} \cdot \rho_{tr_i}\}$ 
7       $\forall i \in W^r : select_i \leftarrow select_i + 1$ 
8      send a task  $T$  to all workers in  $W^r$ 
9      collect replies from workers in  $W^r$  for  $t$  time
10     wait for  $t$  time collecting replies as received from workers in  $W^r$ 
11      $R \leftarrow \{i \in W^r : \text{a reply from } i \text{ was received by time } t\}$ 
12      $\forall i \in R : reply\_select_i \leftarrow reply\_select_i + 1$ 
13     update responsiveness reputation  $\rho_{rs_i}$  of each worker  $i \in W^r$ 
14     audit the received answers with probability  $p_A$ 
15     if the answers were not audited then
16         accept the value  $m$  returned by workers  $R_m \subseteq R$ ,
17         where  $\forall m', \rho_{tr_{R_m}} \geq \rho_{tr_{R_{m'}}$  // weighted majority of workers in  $R$ 
18     else // the master audits
19         foreach  $i \in R$  do
20              $audit\_reply\_select_i \leftarrow audit\_reply\_select_i + 1$ 
21             if  $i \in F$  then  $streak_i \leftarrow 0$  //  $F \subseteq R$  is the set of responsive workers caught cheating
22             else  $correct\_audit_i \leftarrow correct\_audit_i + 1$ ,  $streak_i \leftarrow streak_i + 1$  // honest responsive
23             update truthfulness reputation  $\rho_{tr_i}$  // depending on the type used
24             if  $\rho_{tr_R} = 0$  then  $p_A \leftarrow \min\{1, p_A + \alpha_m\}$ 
25             else
26                  $p'_A \leftarrow p_A + \alpha_m(\rho_{tr_F} / \rho_{tr_R} - \tau)$ 
27                  $p_A \leftarrow \min\{1, \max\{p_A^{min}, p'_A\}\}$ 
28      $\forall i \in W^r : \text{return } \Pi_i$  to worker  $i$  // the payoff of workers in  $W^r \setminus R$  is zero
```

---

if audited,  
update truthfulness  
reputation

# Protocol

---

## Algorithm 1 Master's Algorithm

---

```

1   $p_A \leftarrow x$ , where  $x \in [p_A^{min}, 1]$ 
2  for  $i \leftarrow 0$  to  $N$  do
3       $select_i \leftarrow 0$ ;  $reply\_select_i \leftarrow 0$ ;  $audit\_reply\_select_i \leftarrow 0$ ;  $correct\_audit_i \leftarrow 0$ ;  $streak_i \leftarrow 0$ 
4       $\rho_{rs_i} \leftarrow 1$ ; initialize  $\rho_{tr_i}$  // initially all workers have the same reputation
5  for  $r \leftarrow 1$  to  $\infty$  do
6       $W^r \leftarrow \{i \in \mathcal{N} : i \text{ is chosen as one of the } n \text{ workers with the highest } \rho_i = \rho_{rs_i} \cdot \rho_{tr_i}\}$ 
7       $\forall i \in W^r : select_i \leftarrow select_i + 1$ 
8      send a task  $T$  to all workers in  $W^r$ 
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11      $R \leftarrow \{i \in W^r : \text{a reply from } i \text{ was received by time } t\}$ 
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20              $audit\_reply\_select_i \leftarrow audit\_reply\_select_i + 1$ 
21             if  $i \in F$  then  $streak_i \leftarrow 0$  //  $F \subseteq R$  is the set of responsive workers caught cheating
22             else  $correct\_audit_i \leftarrow correct\_audit_i + 1$ ,  $streak_i \leftarrow streak_i + 1$  // honest responsive
23             update truthfulness reputation  $\rho_{tr_i}$  // depending on the type used
24             if  $\rho_{tr_R} = 0$  then  $p_A \leftarrow \min\{1, p_A + \alpha_m\}$ 
25             else
26                  $p'_A \leftarrow p_A + \alpha_m(\rho_{tr_F} / \rho_{tr_R} - \tau)$ 
27                  $p_A \leftarrow \min\{1, \max\{p_A^{min}, p'_A\}\}$ 
28      $\forall i \in W^r : \text{return } \Pi_i$  to worker  $i$  // the payoff of workers in  $W^r \setminus R$  is zero

```

---

... and  $p_A$

tolerance  
to loss

# Protocol

---

## Algorithm 1 Master's Algorithm

---

```

1   $p_A \leftarrow x$ , where  $x \in [p_A^{min}, 1]$ 
2  for  $i \leftarrow 0$  to  $N$  do
3       $select_i \leftarrow 0$ ;  $reply\_select_i \leftarrow 0$ ;  $audit\_reply\_select_i \leftarrow 0$ ;  $correct\_audit_i \leftarrow 0$ ;  $streak_i \leftarrow 0$ 
4       $\rho_{rs_i} \leftarrow 1$ ; initialize  $\rho_{tr_i}$  // initially all workers have the same reputation
5  for  $r \leftarrow 1$  to  $\infty$  do
6       $W^r \leftarrow \{i \in \mathcal{N} : i \text{ is chosen as one of the } n \text{ workers with the highest } \rho_i = \rho_{rs_i} \cdot \rho_{tr_i}\}$ 
7       $\forall i \in W^r : select_i \leftarrow select_i + 1$ 
8      send a task  $T$  to all workers in  $W^r$ 
9      collect replies from workers in  $W^r$  for  $t$  time
10     wait for  $t$  time collecting replies as received from workers in  $W^r$ 
11      $R \leftarrow \{i \in W^r : \text{a reply from } i \text{ was received by time } t\}$ 
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13     update responsiveness reputation  $\rho_{rs_i}$  of each worker  $i \in W^r$ 
14     audit the received answers with probability  $p_A$ 
15     if the answers were not audited then
16         accept the value  $m$  returned by workers  $R_m \subseteq R$ ,
17         where  $\forall m', \rho_{tr_{R_m}} \geq \rho_{tr_{R_{m'}}$  // weighted majority of workers in  $R$ 
18     else // the master audits
19         foreach  $i \in R$  do
20              $audit\_reply\_select_i \leftarrow audit\_reply\_select_i + 1$ 
21             if  $i \in F$  then  $streak_i \leftarrow 0$  //  $F \subseteq R$  is the set of responsive workers caught cheating
22             else  $correct\_audit_i \leftarrow correct\_audit_i + 1$ ,  $streak_i \leftarrow streak_i + 1$  // honest responsive
23             update truthfulness reputation  $\rho_{tr_i}$  // depending on the type used
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25             else
26                  $p'_A \leftarrow p_A + \alpha_m(\rho_{tr_F} / \rho_{tr_R} - \tau)$ 
27                  $p_A \leftarrow \min\{1, \max\{p_A^{min}, p'_A\}\}$ 
28      $\forall i \in W^r : \text{return } \Pi_i$  to worker  $i$  // the payoff of workers in  $W^r \setminus R$  is zero

```

---

pay/penalize  
accordingly

tolerance  
to loss



# Protocol

---

**Algorithm 2** Algorithm for Rational Worker  $i$ 

---

```
1   $p_{Ci} \leftarrow y$ , where  $y \in [0, 1]$ 
2  repeat forever
3      wait for a task  $T$  from the master
4      if available then
5          decide whether to cheat or not independently with distribution  $P(\text{cheat}) = p_{Ci}$ 
6          if the decision was to cheat then
7              send arbitrary solution to the master
8              get payoff  $\Pi_i$ 
9               $p_{Ci} \leftarrow \max\{0, \min\{1, p_{Ci} + \alpha_w(\Pi_i - a_i)\}\}$ 
10         else
11             send compute( $T$ ) to the master
12             get payoff  $\Pi_i$ 
13              $p_{Ci} \leftarrow \max\{0, \min\{1, p_{Ci} - \alpha_w(\Pi_i - WC_{\mathcal{T}} - a_i)\}\}$ 
```

---

# Protocol

cheat with  
probability  $p_C$

---

**Algorithm 2** Algorithm for Rational Worker  $i$ 

---

```
1   $p_{Ci} \leftarrow y$ , where  $y \in [0, 1]$ 
2  repeat forever
3      wait for a task  $T$  from the master
4      if available then
5          decide whether to cheat or not independently with distribution  $P(\text{cheat}) = p_{Ci}$ 
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8              get payoff  $\Pi_i$ 
9               $p_{Ci} \leftarrow \max\{0, \min\{1, p_{Ci} + \alpha_w(\Pi_i - a_i)\}\}$ 
10         else
11             send compute( $T$ ) to the master
12             get payoff  $\Pi_i$ 
13              $p_{Ci} \leftarrow \max\{0, \min\{1, p_{Ci} - \alpha_w(\Pi_i - WC_{\mathcal{T}} - a_i)\}\}$ 
```

---



# Protocol

---

**Algorithm 2** Algorithm for Rational Worker  $i$ 

---

```
1   $p_{Ci} \leftarrow y$ , where  $y \in [0, 1]$ 
2  repeat forever
3      wait for a task  $T$  from the master
4      if available then
5          decide whether to cheat or not independently with distribution  $P(\text{cheat}) = p_{Ci}$ 
6          if the decision was to cheat then
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8              get payoff  $\Pi_i$ 
9               $p_{Ci} \leftarrow \max\{0, \min\{1, p_{Ci} + \alpha_w(\Pi_i - a_i)\}\}$ 
10         else
11             send compute( $T$ ) to the master
12             get payoff  $\Pi_i$ 
13              $p_{Ci} \leftarrow \max\{0, \min\{1, p_{Ci} - \alpha_w(\Pi_i - WC_T - a_i)\}\}$ 
```

---

cheat with  
probability  $p_C$

update  $p_C$

profit  
aspiration

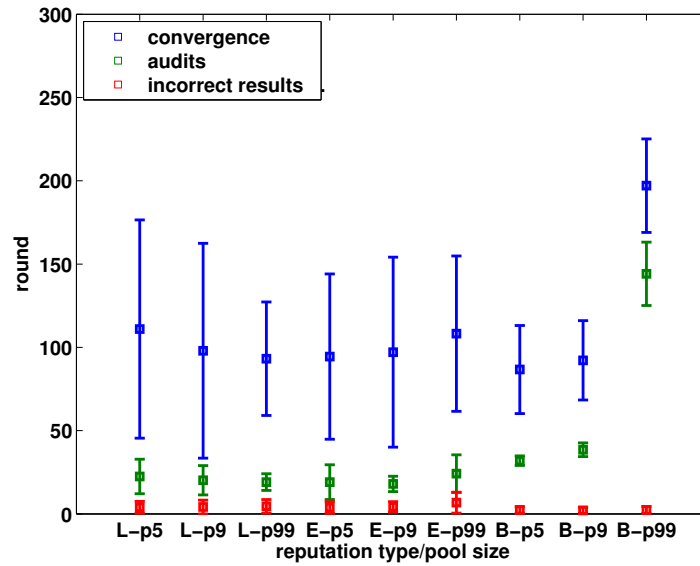
# Feasibility without rationals

**Theorem 3.** *Consider a system in which workers are either altruistic or malicious and there is at least one altruistic worker  $i$  with  $d_i = 1$  in the pool. Eventual correctness is satisfied if the mechanism of Algorithm 1 is used with the responsiveness reputation and any of the truthfulness reputations LINEAR or EXPONENTIAL.*

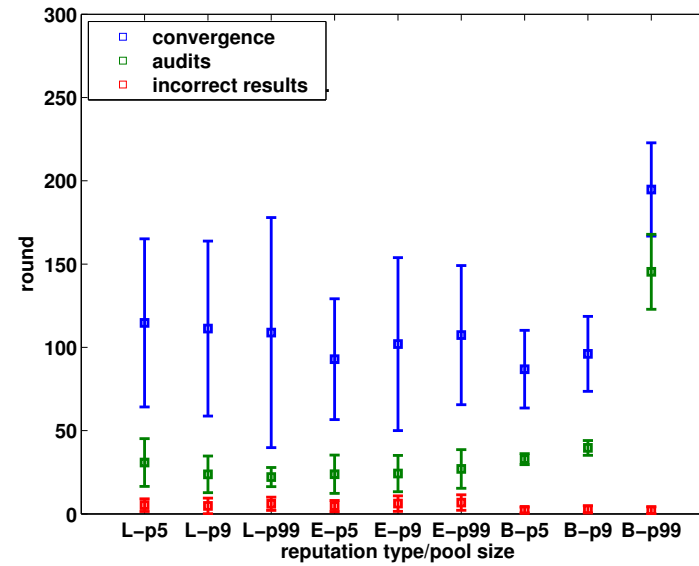
**Theorem 4.** *Consider a system in which workers are either altruistic or malicious and there is at least one altruistic worker  $i$  with  $d_i = 1$  in the pool. In this system, the mechanism of Algorithm 1 is used with the responsiveness reputation and the truthfulness reputation BOINC. Then, eventual correctness is satisfied if and only if the number of altruistic workers with  $d_j < 1$  is smaller than  $n$ .*

# Simulations: workers always available (d=1)

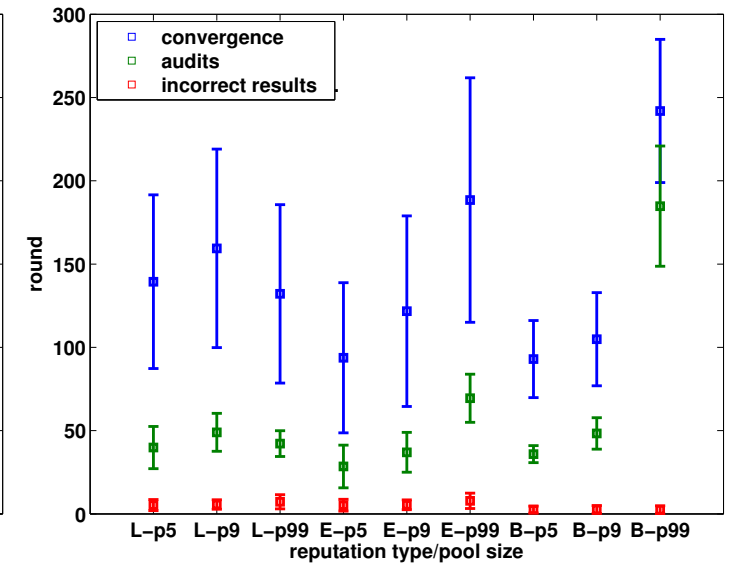
$n=9$ , convergence:  $p_A = p_{Amin} = 0.01$



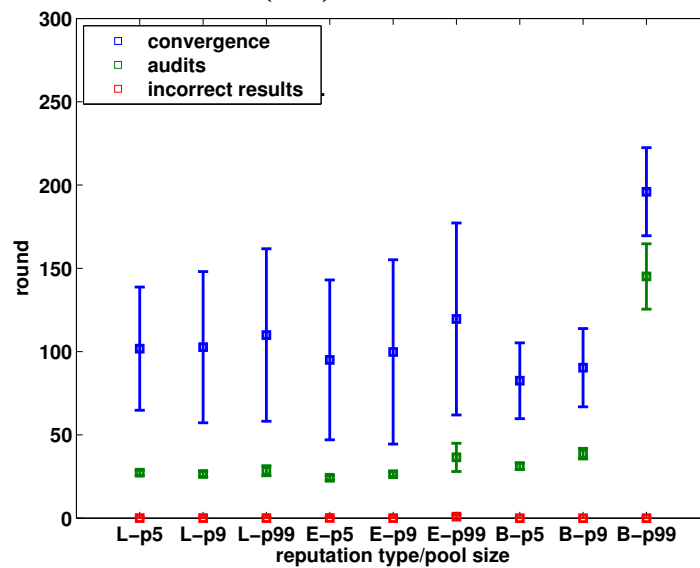
(a1)



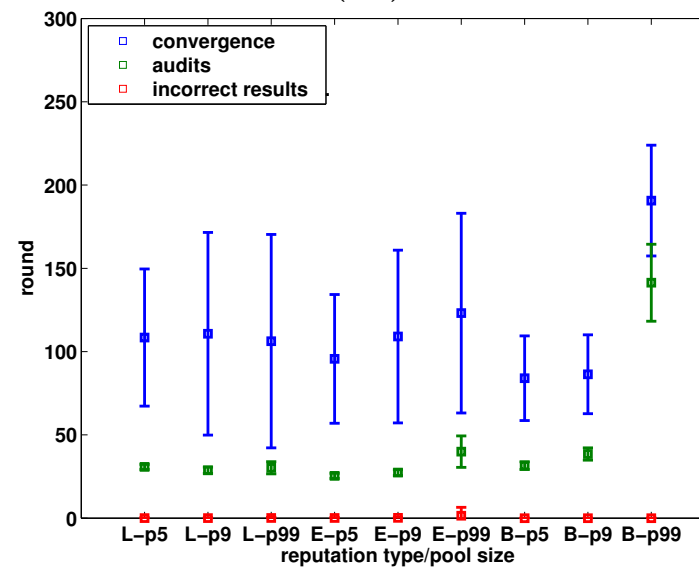
(b1)



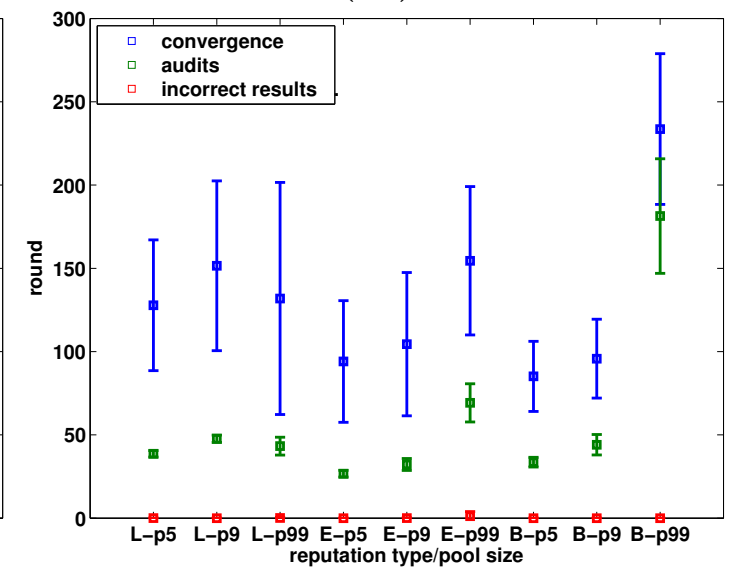
(c1)



(a2)



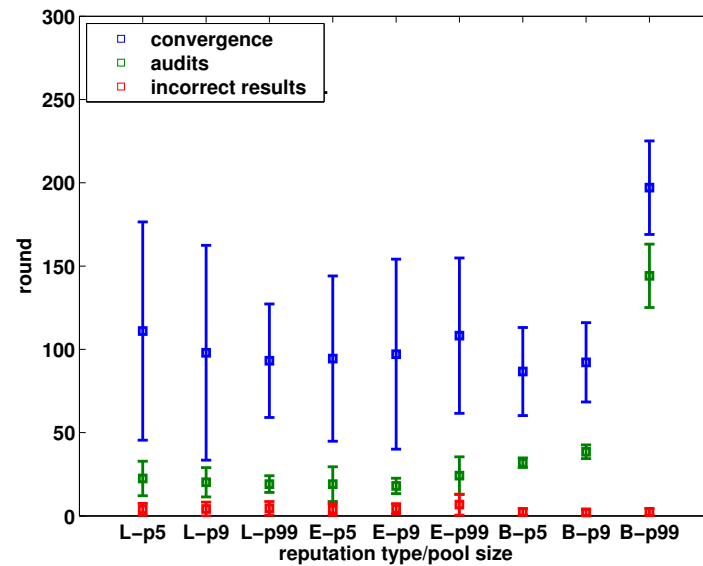
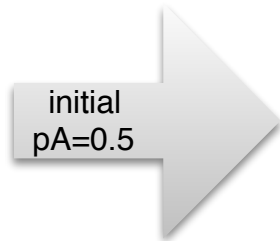
(b2)



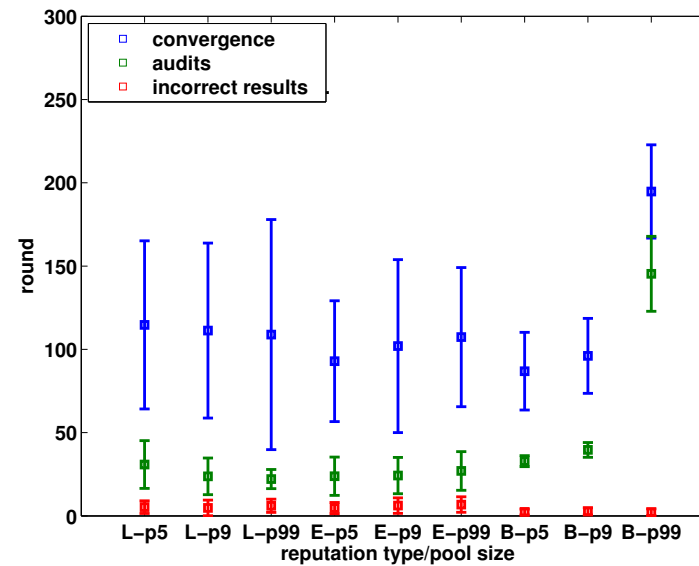
(c2)

# Simulations: workers always available (d=1)

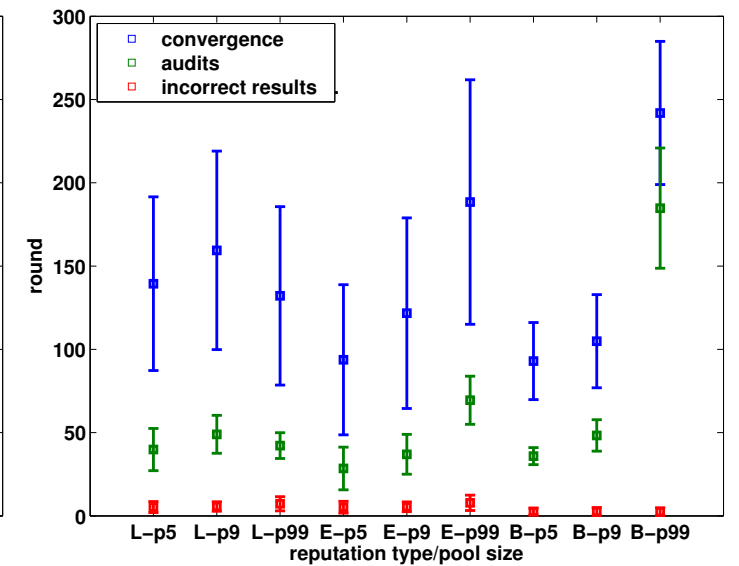
$n=9$ , convergence:  $pA = pA_{min} = 0.01$



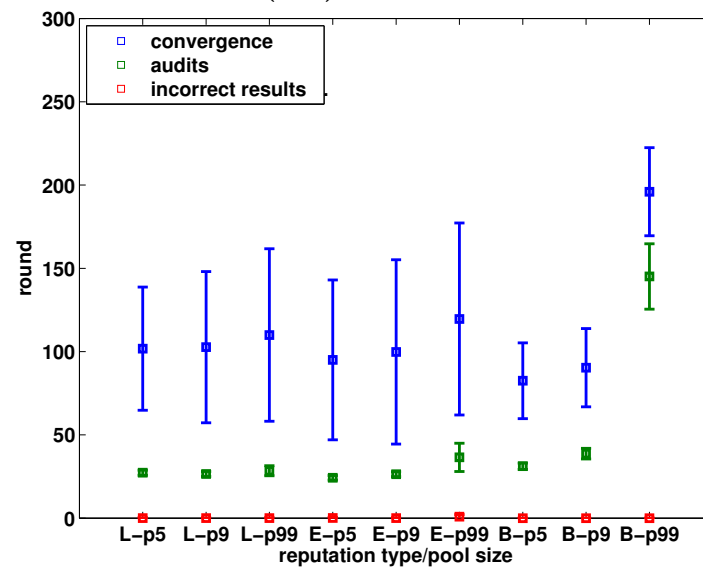
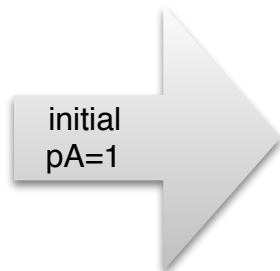
(a1)



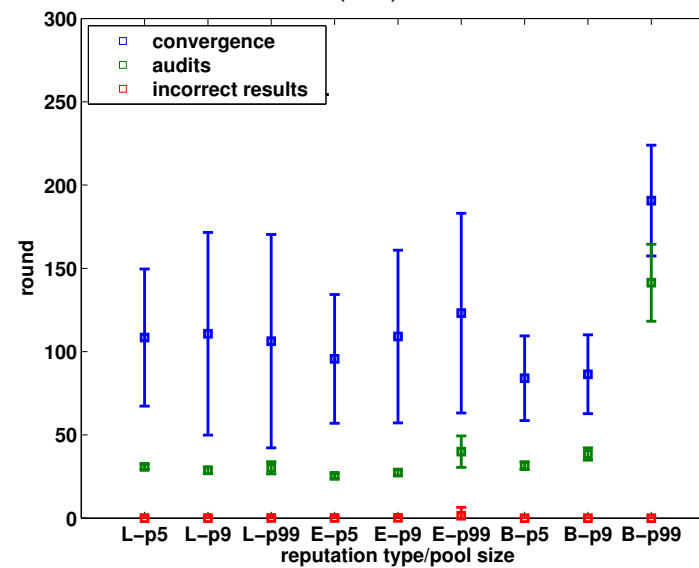
(b1)



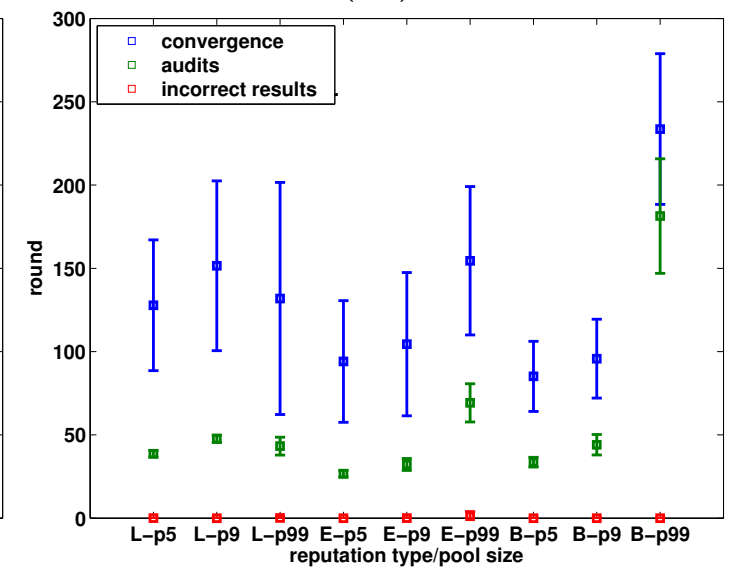
(c1)



(a2)



(b2)



(c2)

# rational / # malicious =

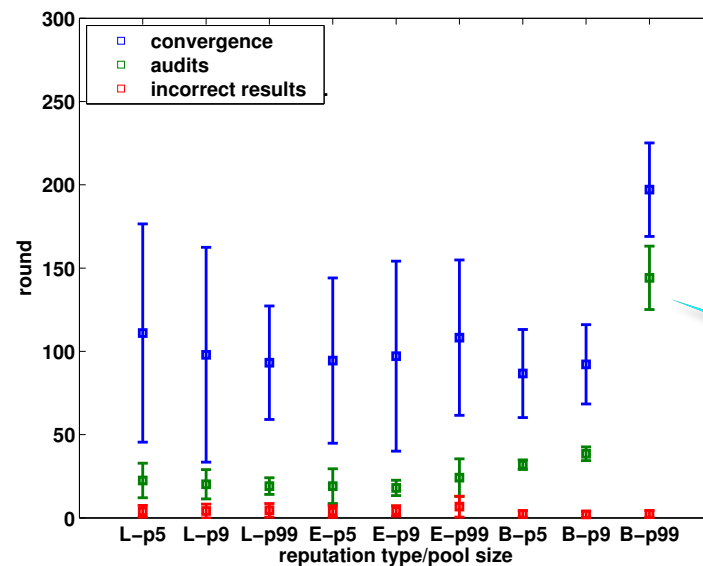
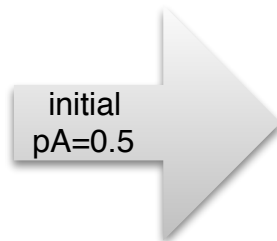
5/4

4/5

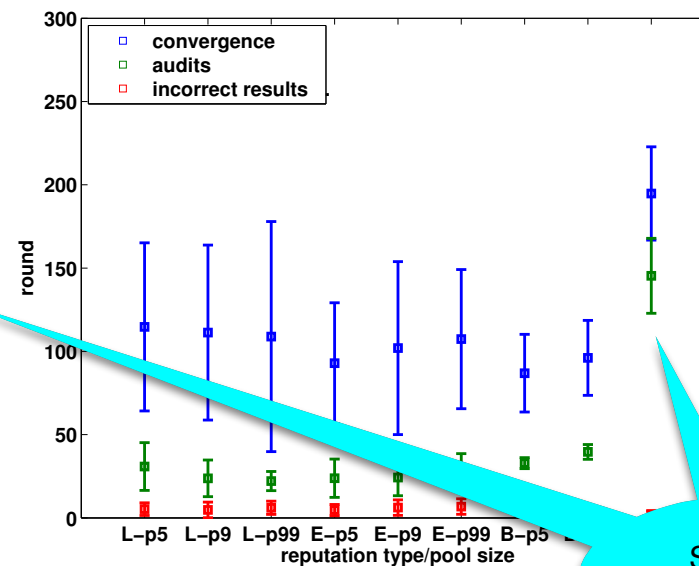
1/8

# Simulations: workers always available (d=1)

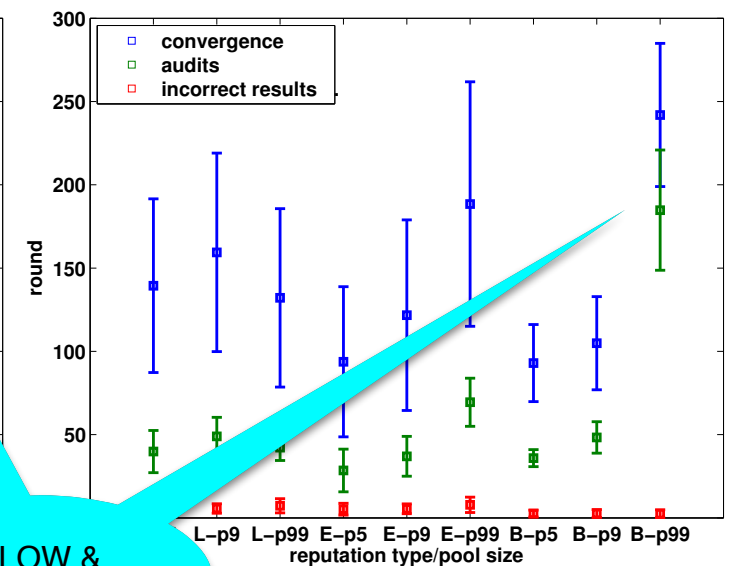
$n=9$ , convergence:  $pA = pA_{\min} = 0.01$



(a1)

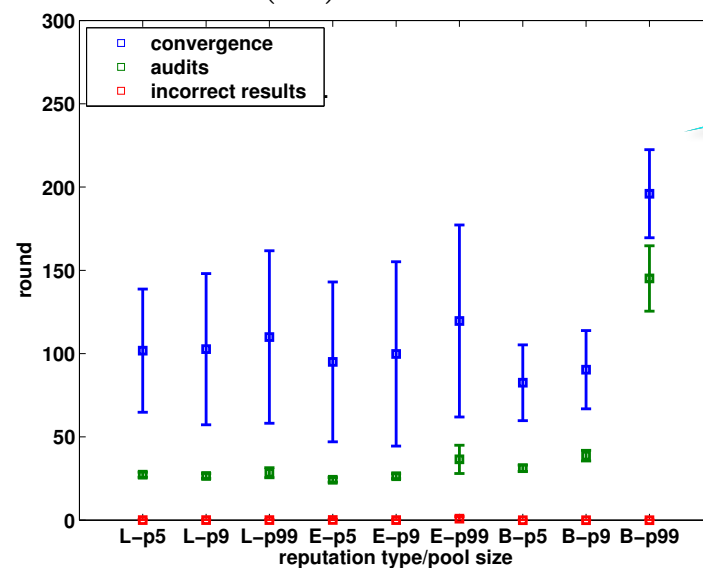
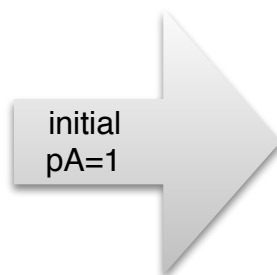


(b1)

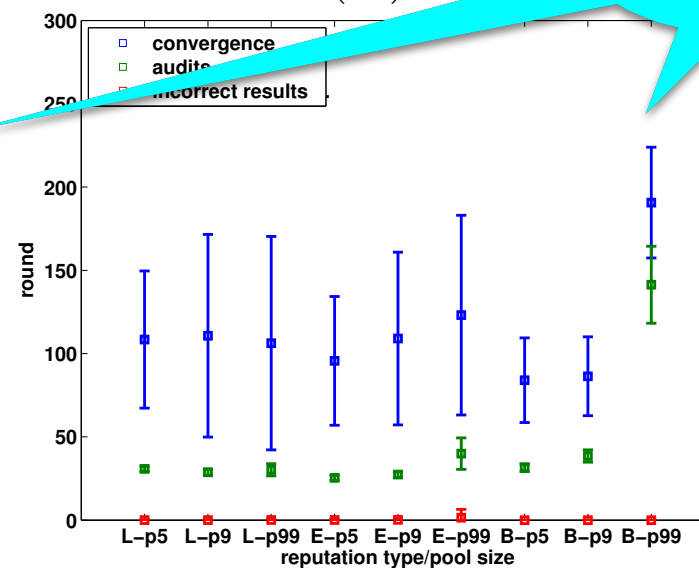


(c1)

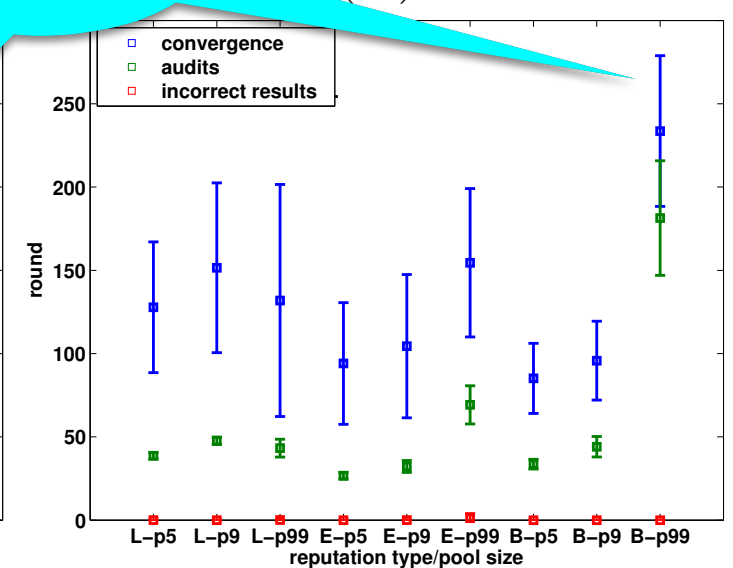
SLOW &  
EXPENSIVE



(a2)



(b2)



(c2)

# rational / # malicious =

5/4

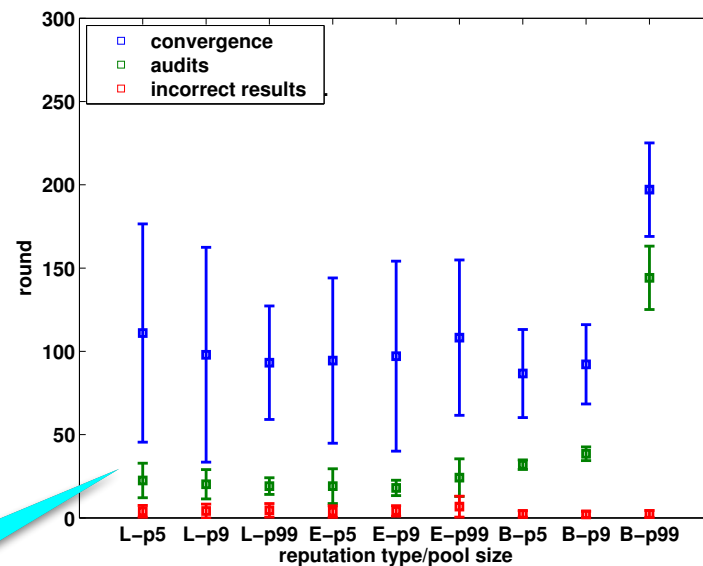
4/5

1/8

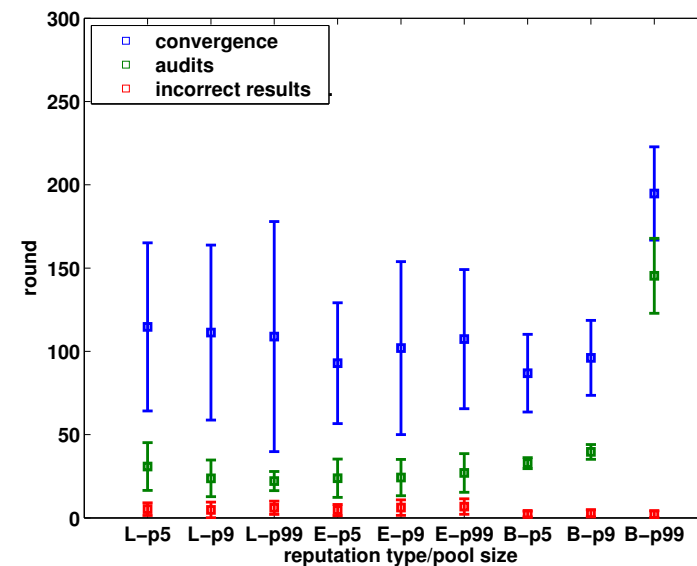
# Simulations: workers always available (d=1)

$n=9$ , convergence:  $pA = pA_{min} = 0.01$

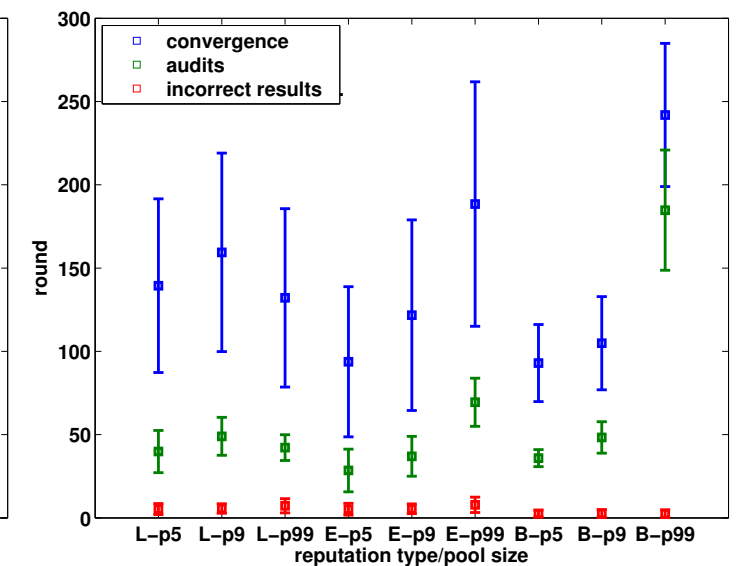
initial  
 $pA=0.5$



(a1)



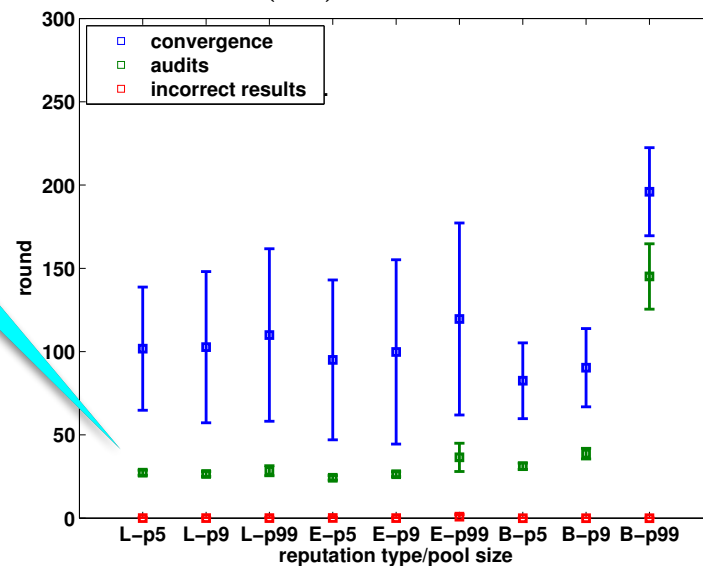
(b1)



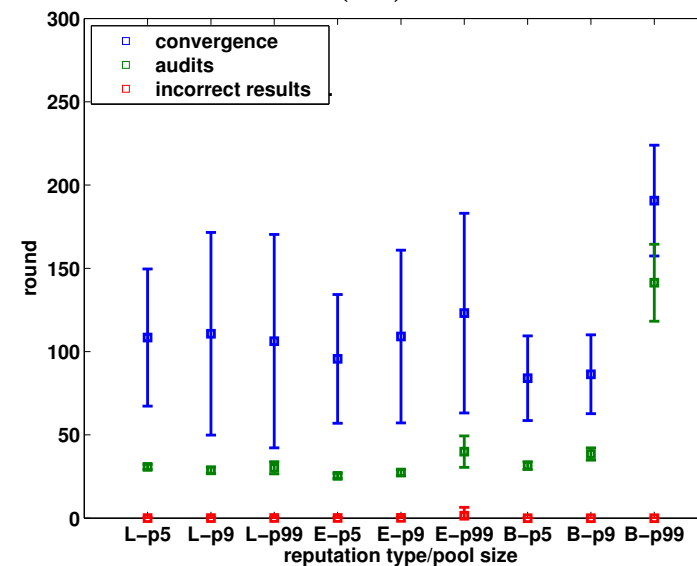
(c1)

LESS  
AUDITS

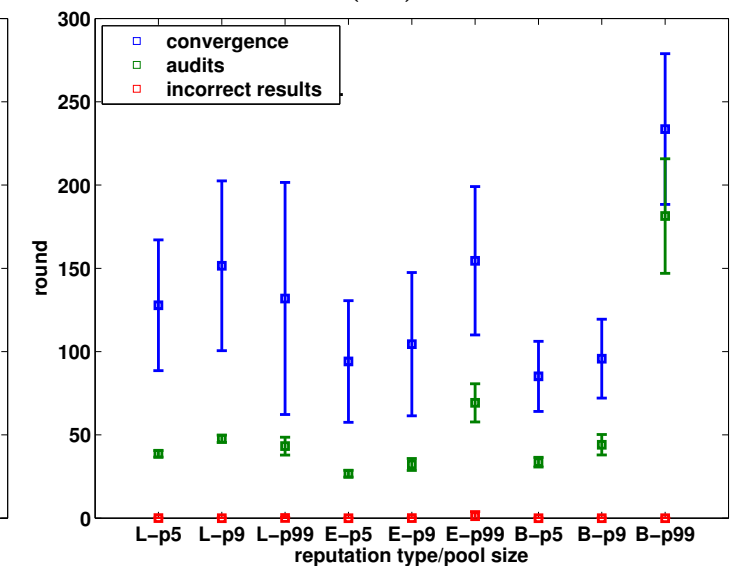
initial  
 $pA=1$



(a2)



(b2)



(c2)

# rational / # malicious =

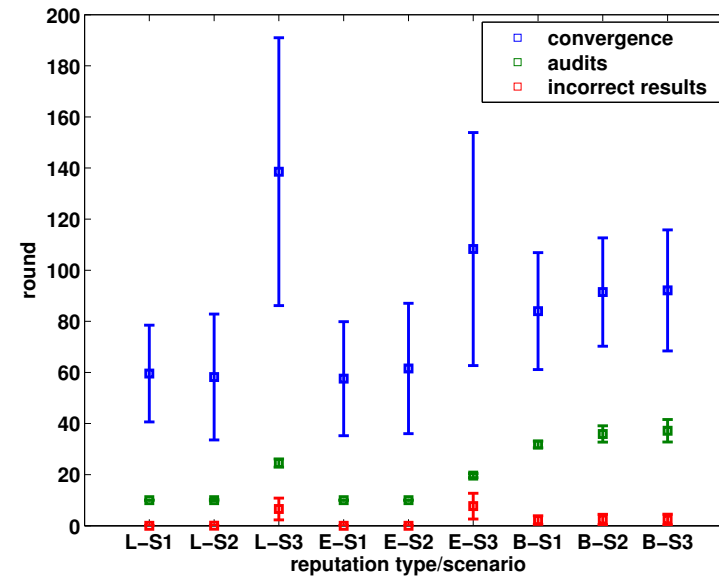
5/4

4/5

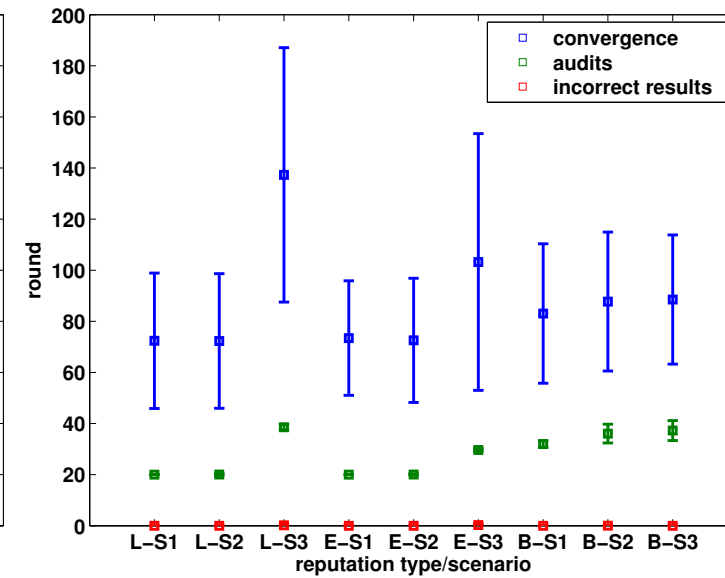
1/8

# Simulations: workers partially available ( $d \leq 1$ )

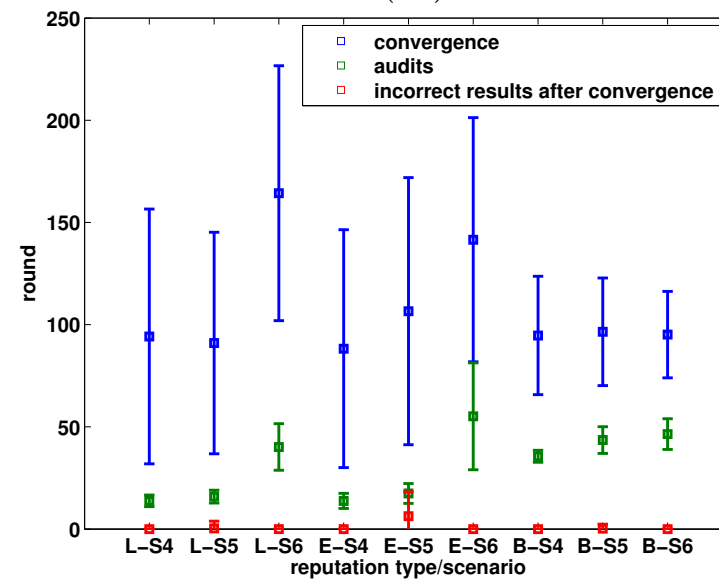
$N=9$ ,  $n=5$ , convergence:  $p_A = p_{Amin} = 0.01$



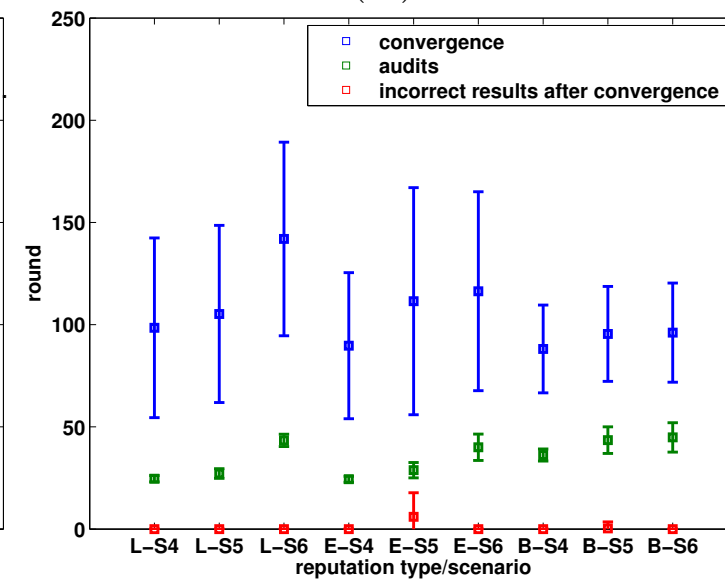
(a1)



(b1)



(a2)

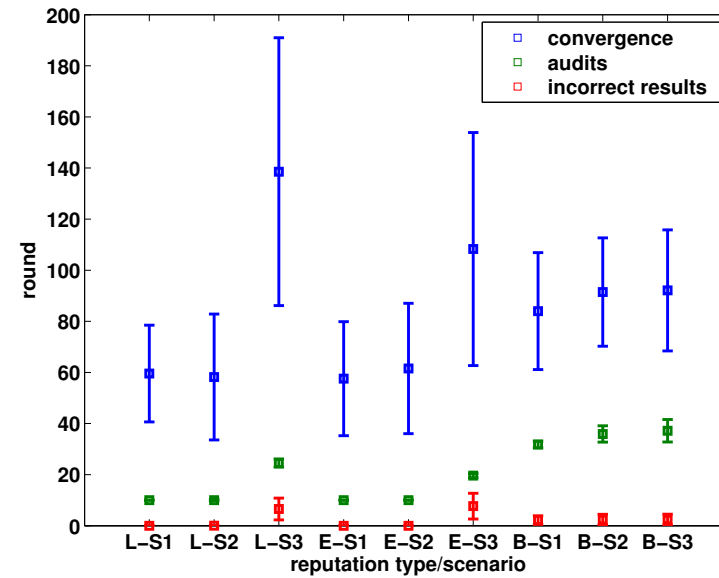


(b2)

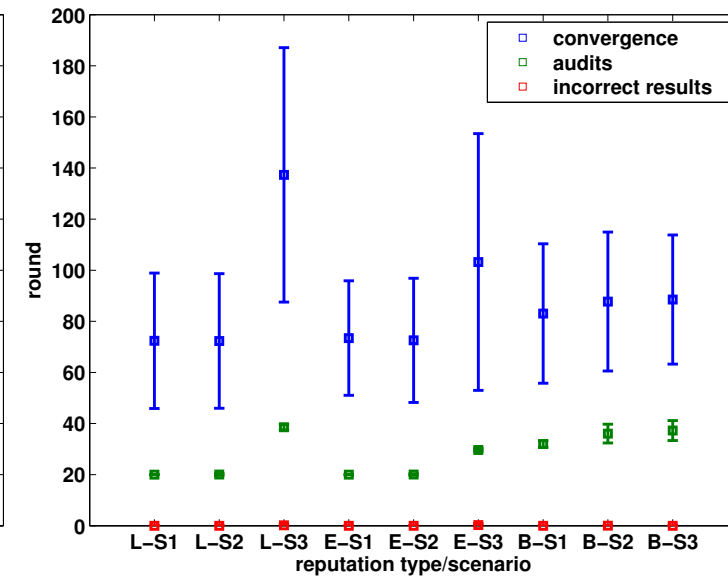
# Simulations: workers partially available ( $d \leq 1$ )

$N=9$ ,  $n=5$ , convergence:  $pA = pA_{min} = 0.01$

	M	A
S1		9)d=1
S2		1)d=1 8)d=0.5
S3	8)d=0.5	1)d=1

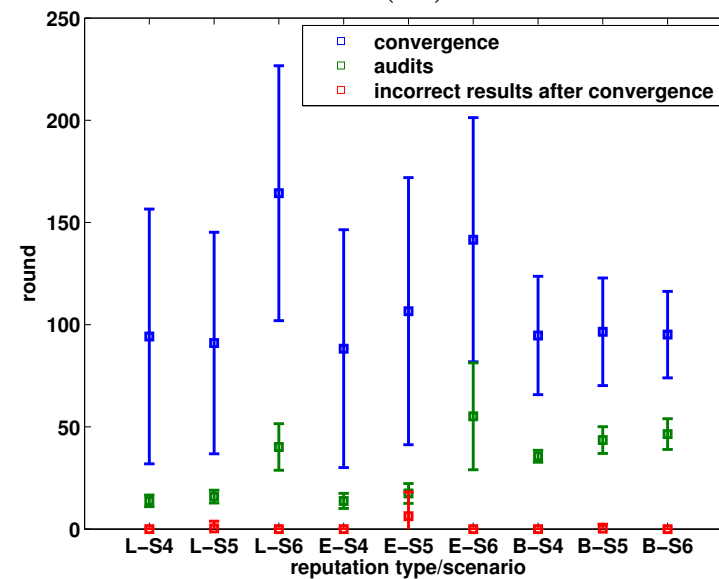


(a1)

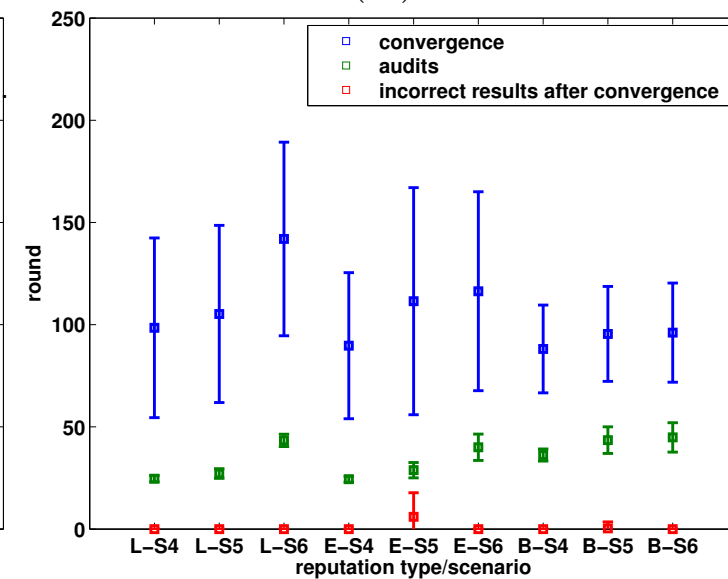


(b1)

	M	R
S4		9)d=1
S5		1)d=1 8)d=0.5
S6	8)d=0.5	1)d=1



(a2)



(b2)

initial  $pA =$

0.5

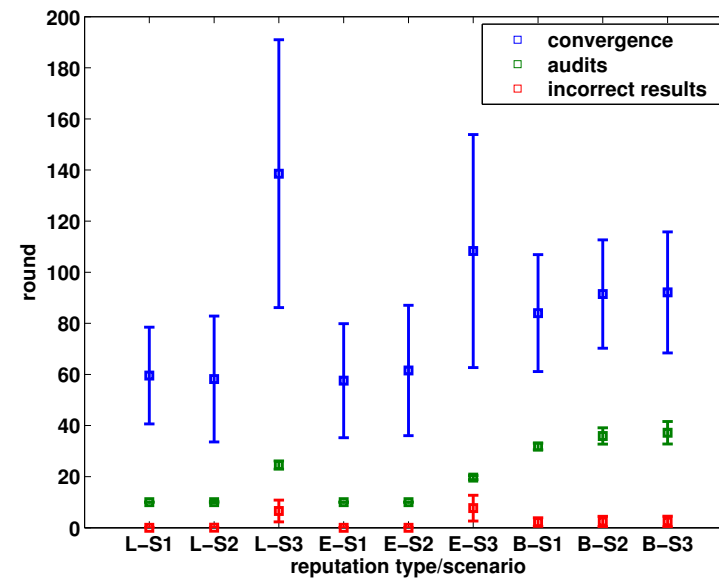
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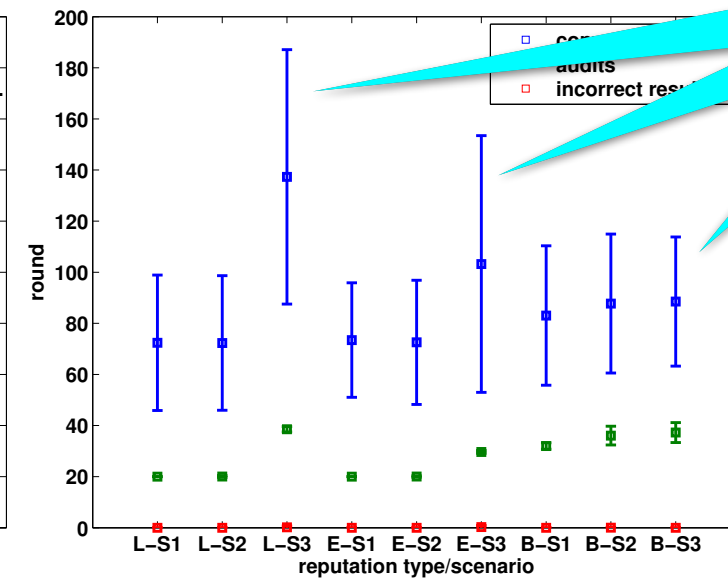
# Simulations: workers partially available ( $d \leq 1$ )

$N=9$ ,  $n=5$ , convergence:  $pA = pA_{min} = 0.01$

	M	A
S1		9)d=1
S2		1)d=1 8)d=0.5
S3	8)d=0.5	1)d=1

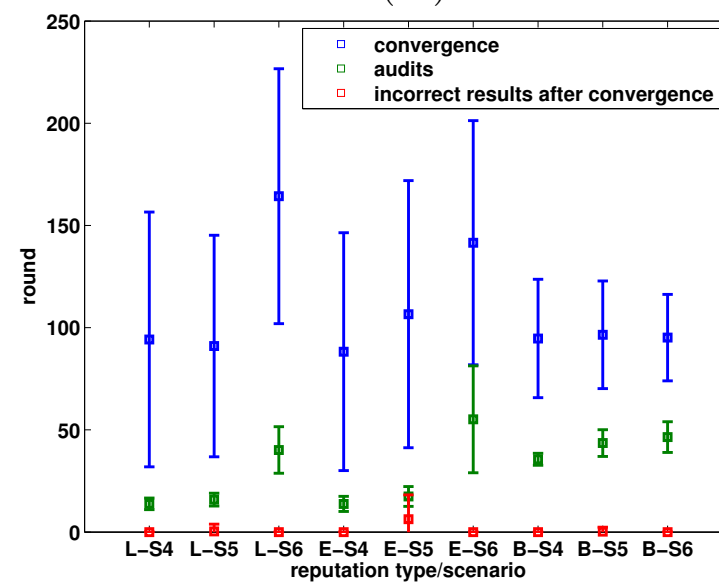


(a1)

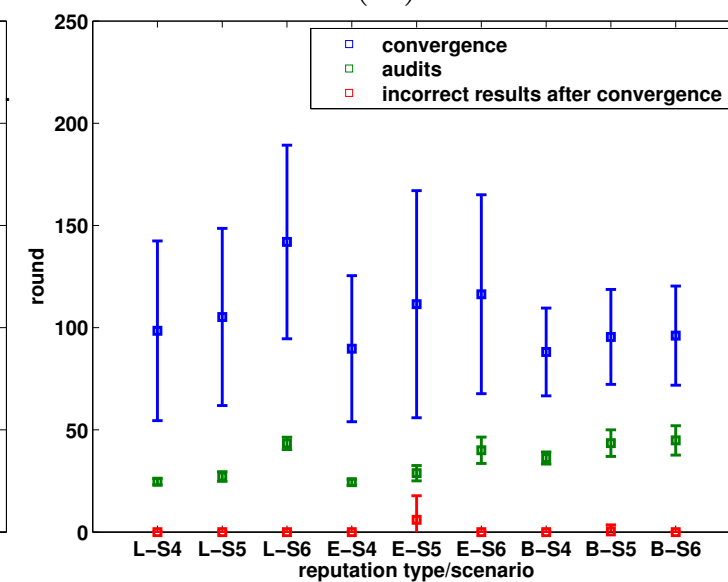


(b1)

	M	R
S4		9)d=1
S5		1)d=1 8)d=0.5
S6	8)d=0.5	1)d=1



(a2)



(b2)

initial  $pA =$

0.5

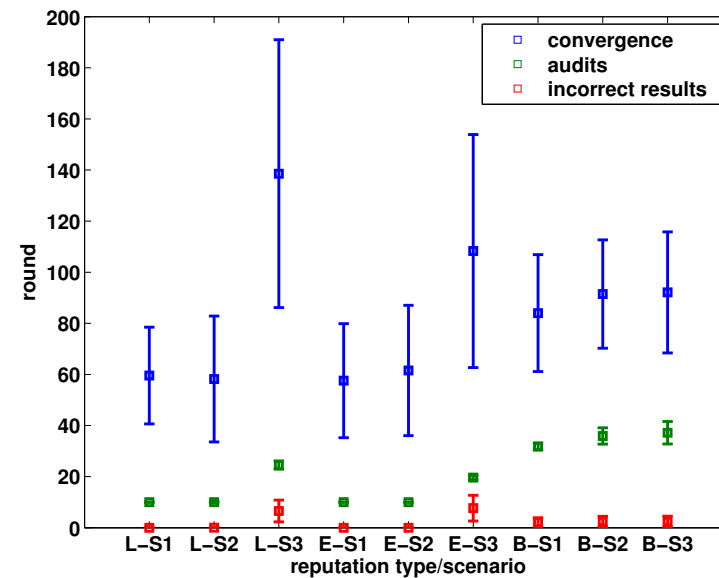
1

WITH  
LOTS OF MALICIOUS  
BOINC IS BETTER

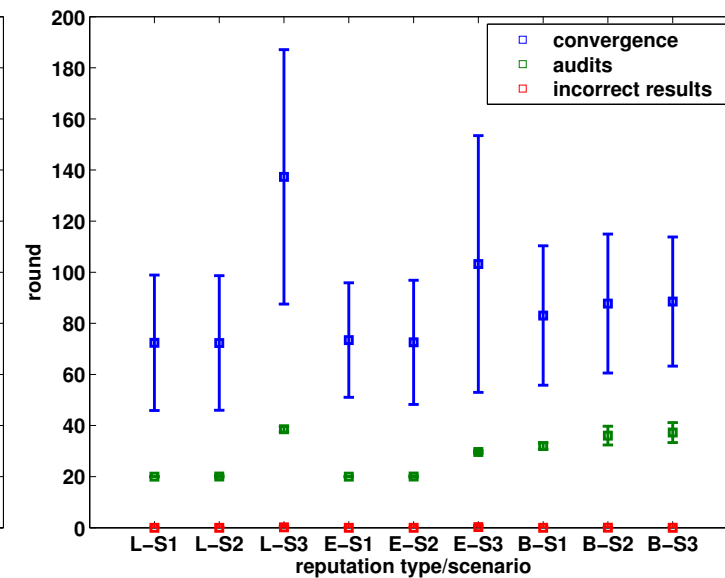
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S1		9)d=1
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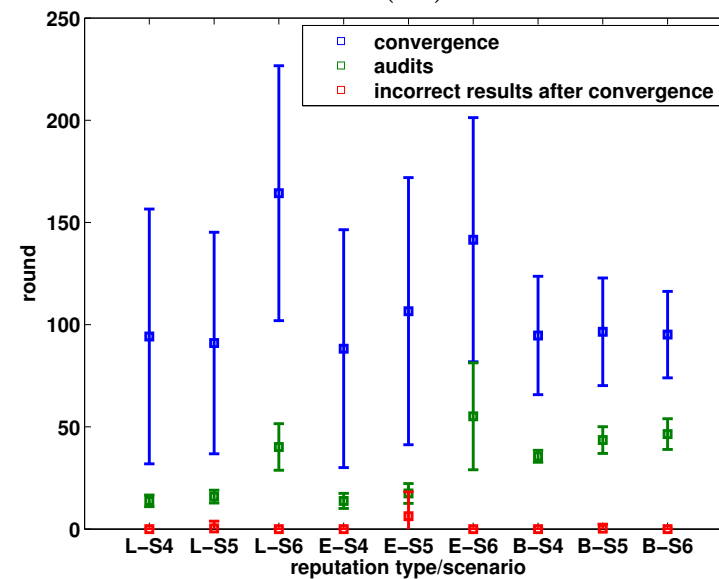


(a1)

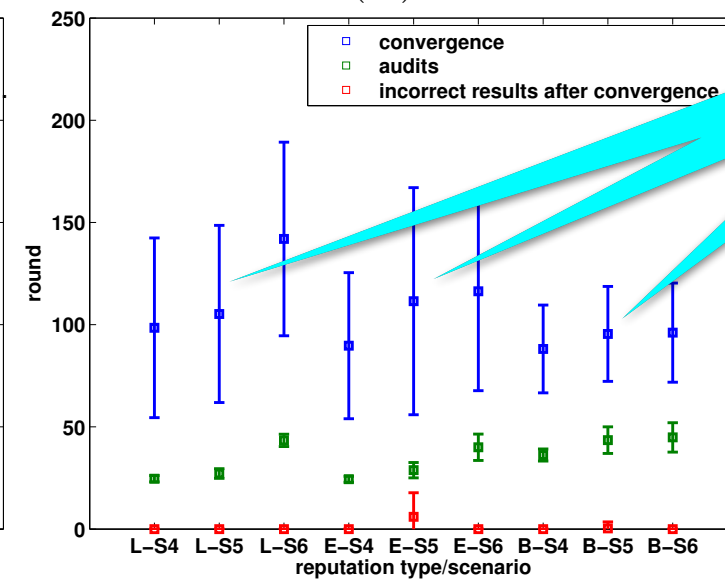


(b1)

	M	R
S4		9)d=1
S5		1)d=1 8)d=0.5
S6	8)d=0.5	1)d=1



(a2)



(b2)

CONVERGENCE  
EVEN WITH  
LOW AVAILABILITY

initial  $pA =$

0.5

1

# Ongoing and future work

- Application of repeated games framework for provable guarantees in multiround computations.
- Experimental comparison of both approaches.
- Integration of our mechanisms into emBoinc.

Thank you!